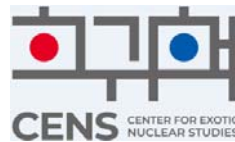


Lunch Seminar of the Center for Exotic Nuclear Studies , the Institute for Basic Science, 2 September 2020.

우리들의 시작과 그 출발점들  
The starting points of our view at CENS

문 창범  
MOON Chang-Bum



- 1 배경: 핵주기율표
- 2 시작점
- 3 출발선에 선 핵종들
- 4 갈 길

말



글



# 1. 배경: 핵주기율

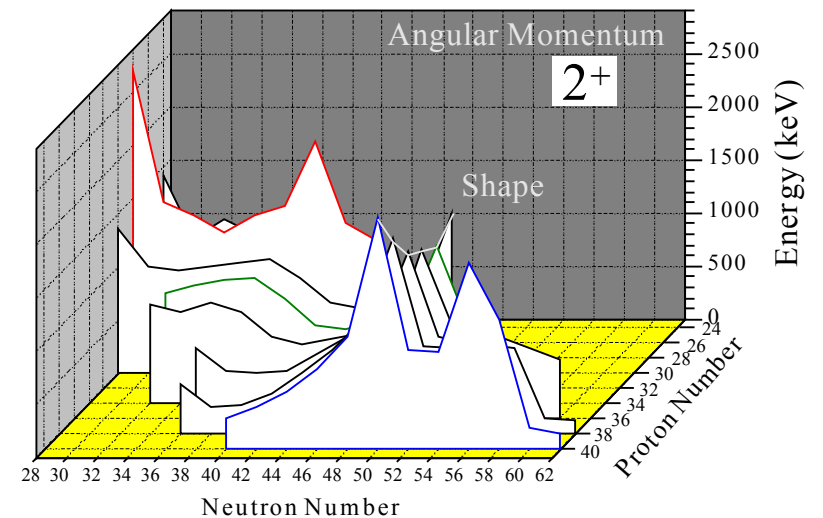
Science is centered on the search for spatiotemporal patterns because nature is organized around

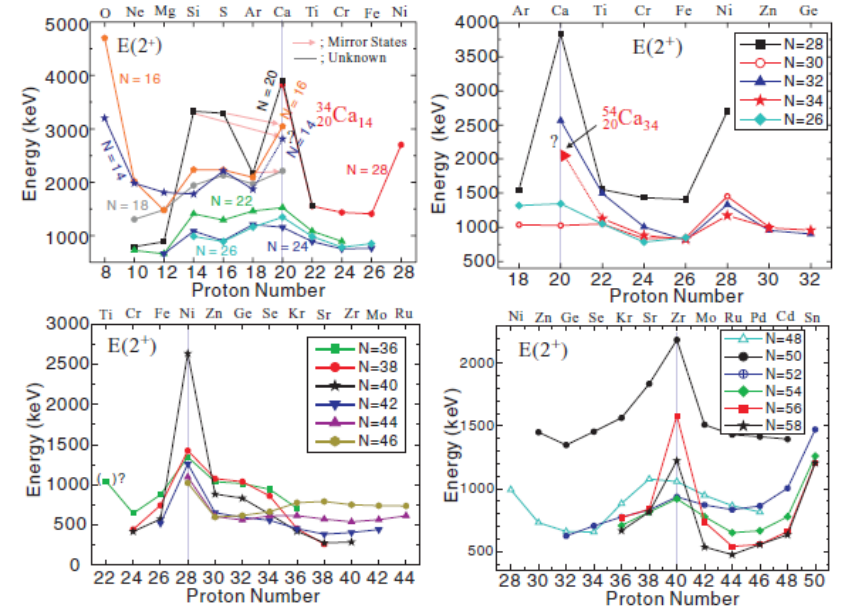
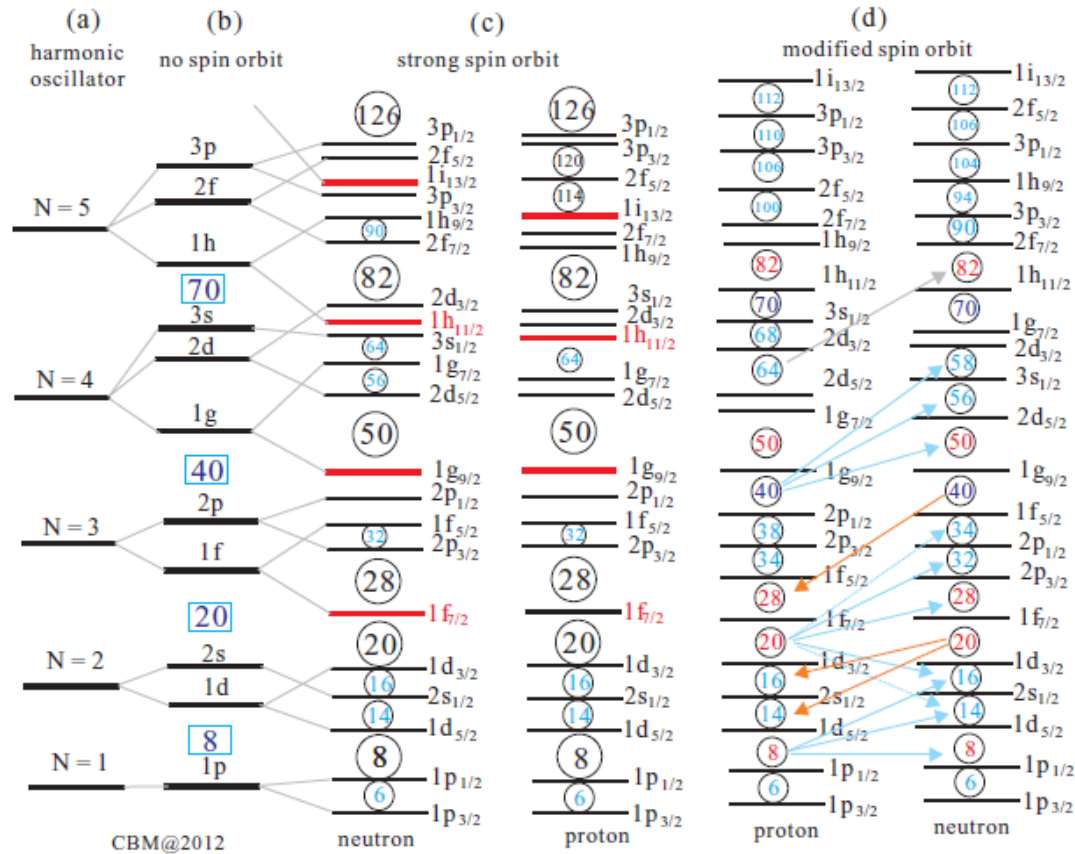
**configurations (spatial patterns) and rhythms (temporal patterns).**

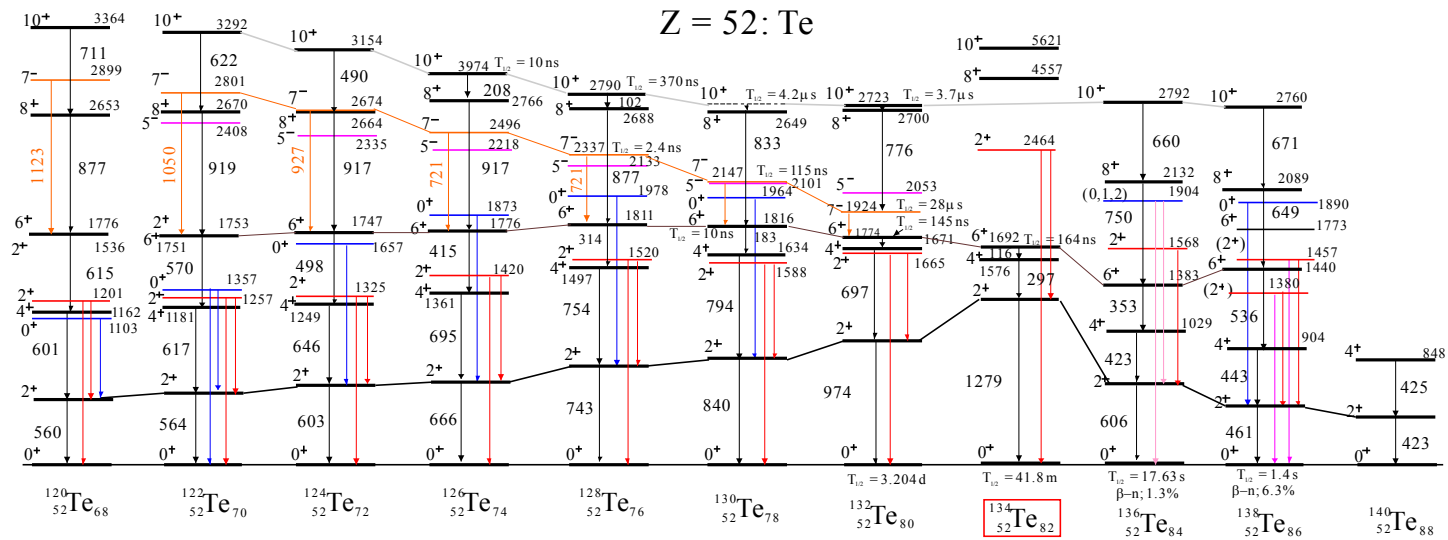
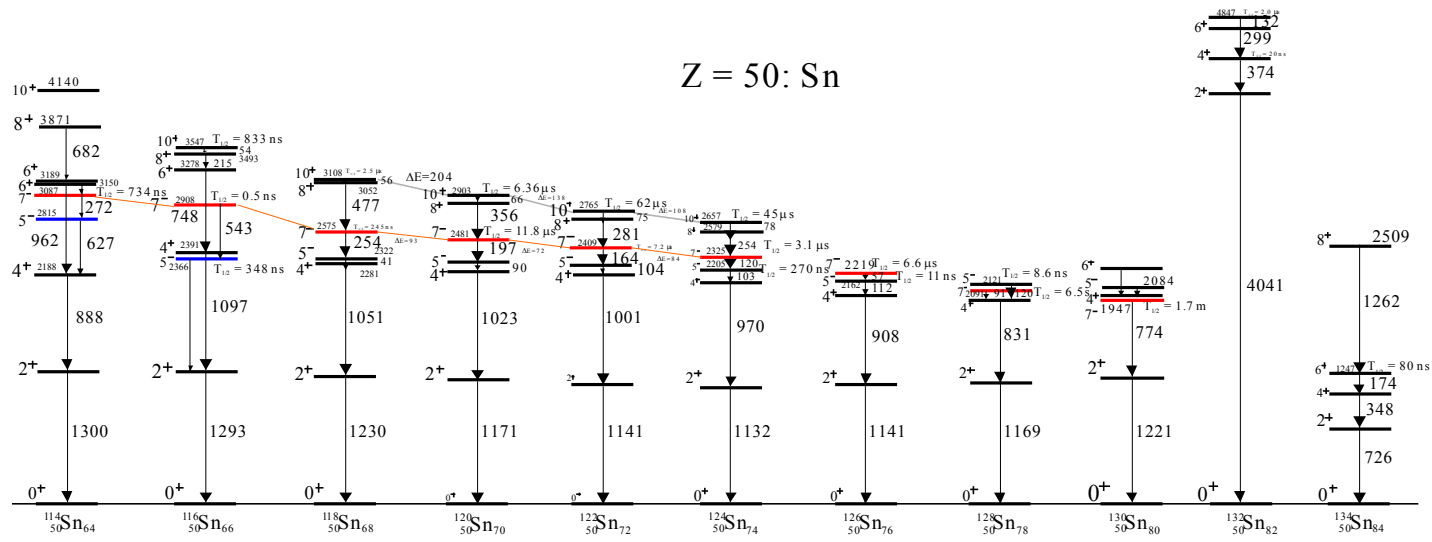
규칙성 => 눈으로 듣고 귀로 본다

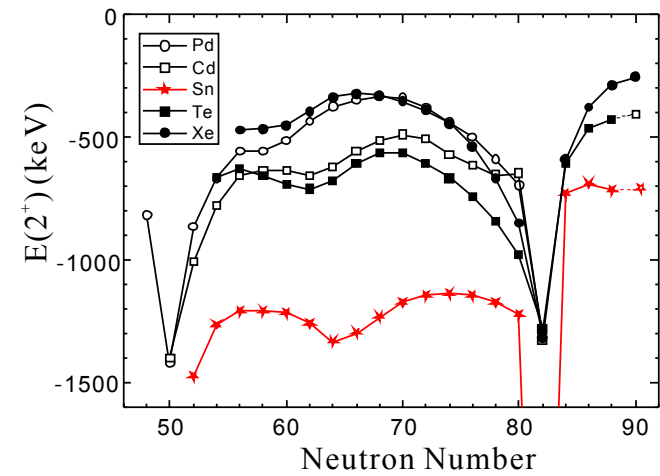
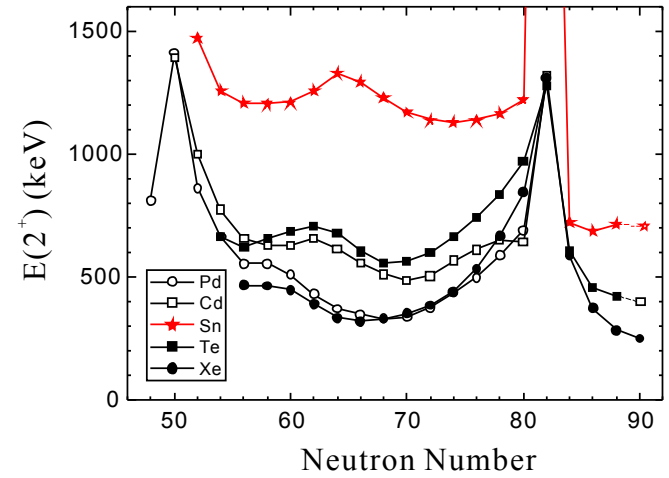
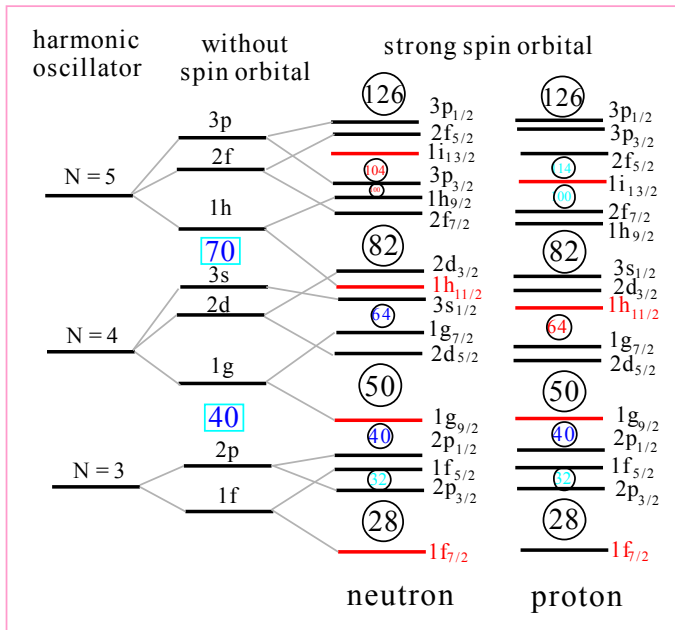
**Configuration is arrangement of elements (nucleons, atoms, molecules, cells and so forth) in space, combined with the properties or attributes of each element, such as velocity (momentum), mass (energy) or shape (force).**

**Pattern means the change to a configuration over a period of time, or a configuration is a cross section of a dynamic pattern at any moment of time.**

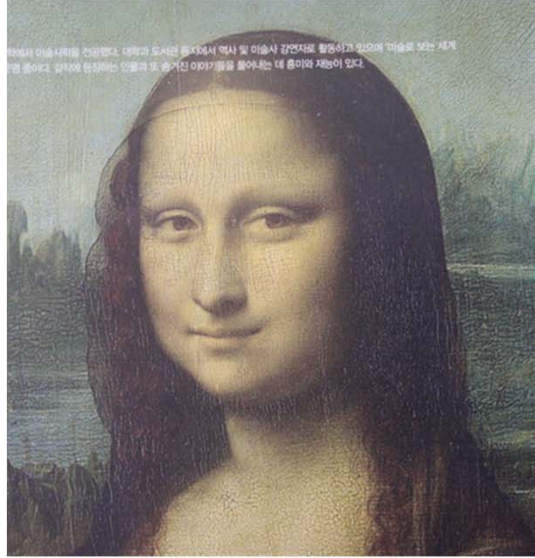


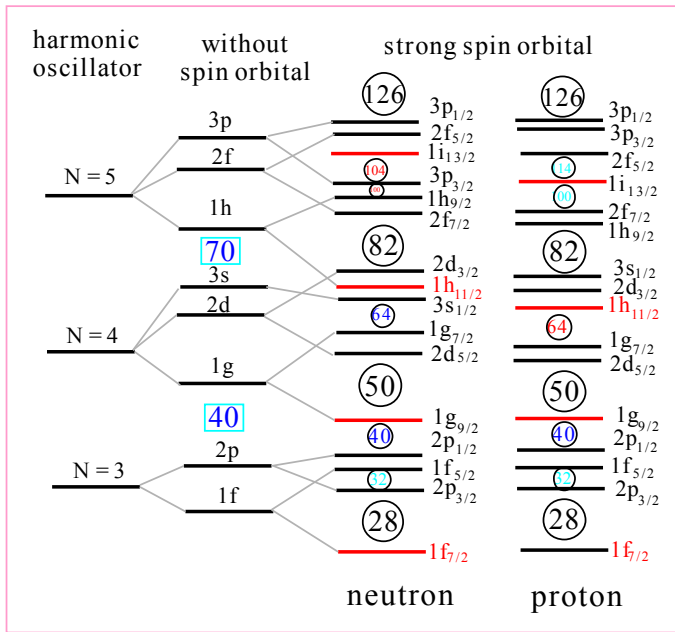




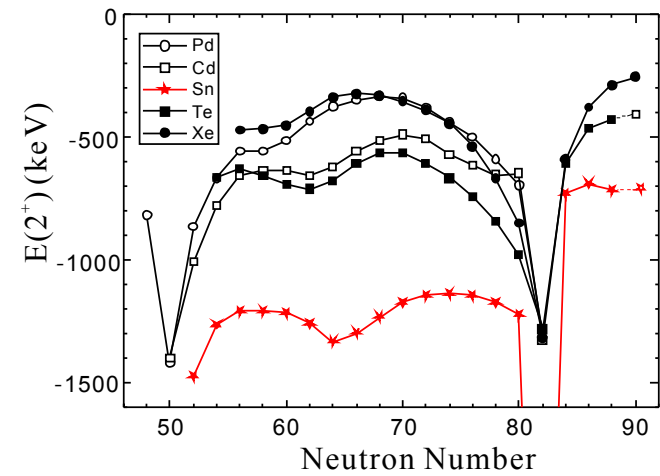
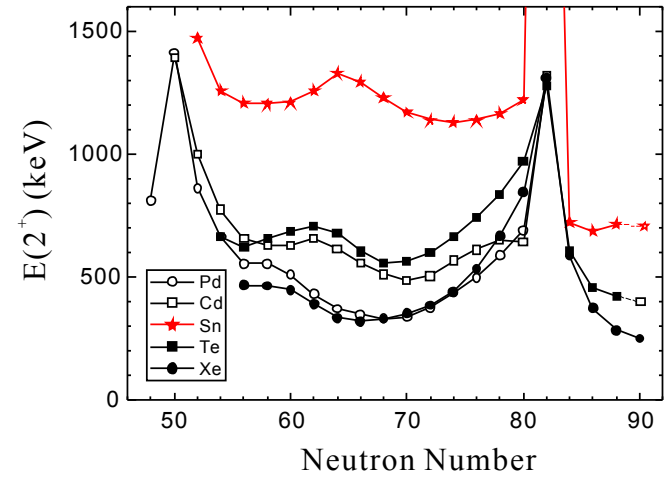








Mapping the Mind by Rita Carter

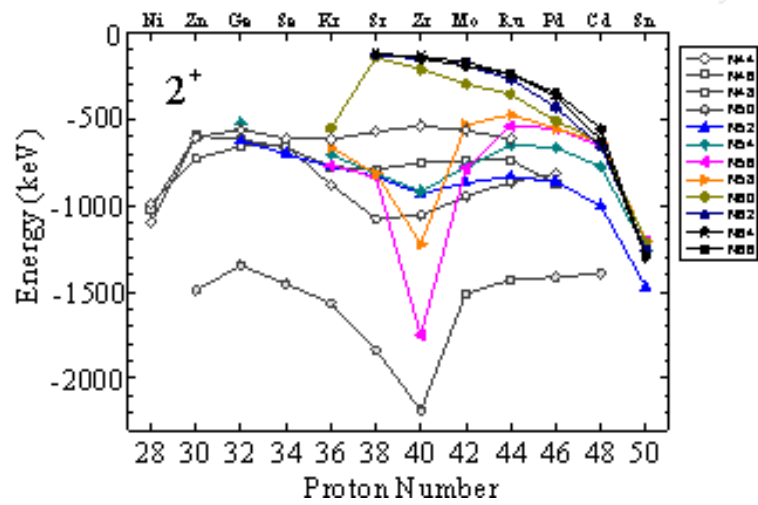
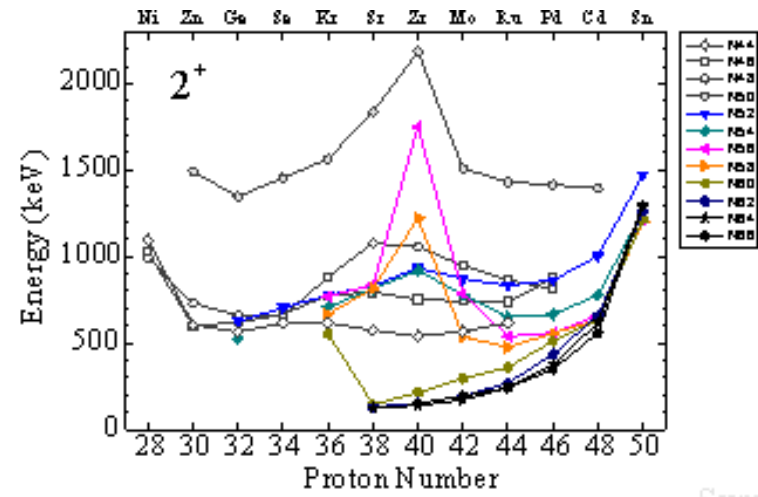




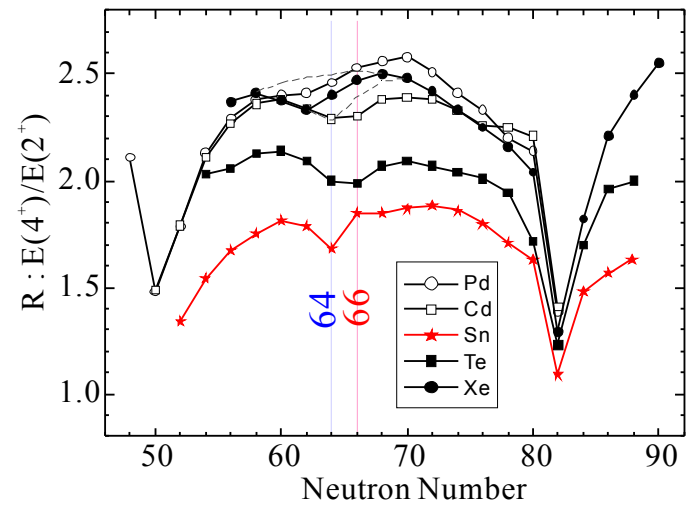
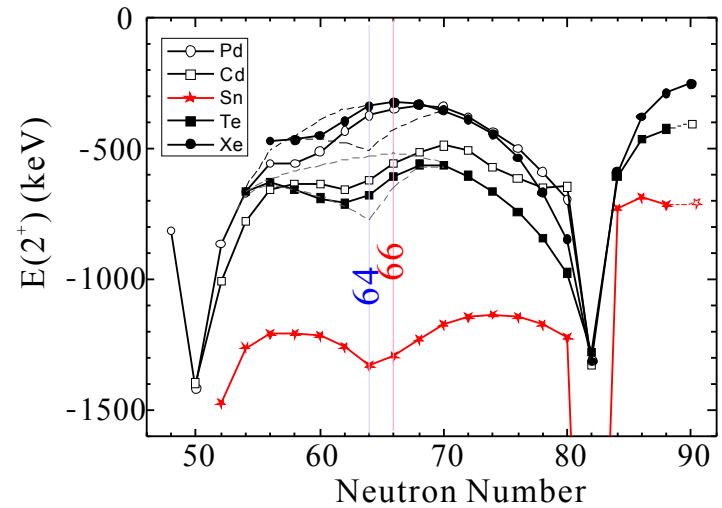
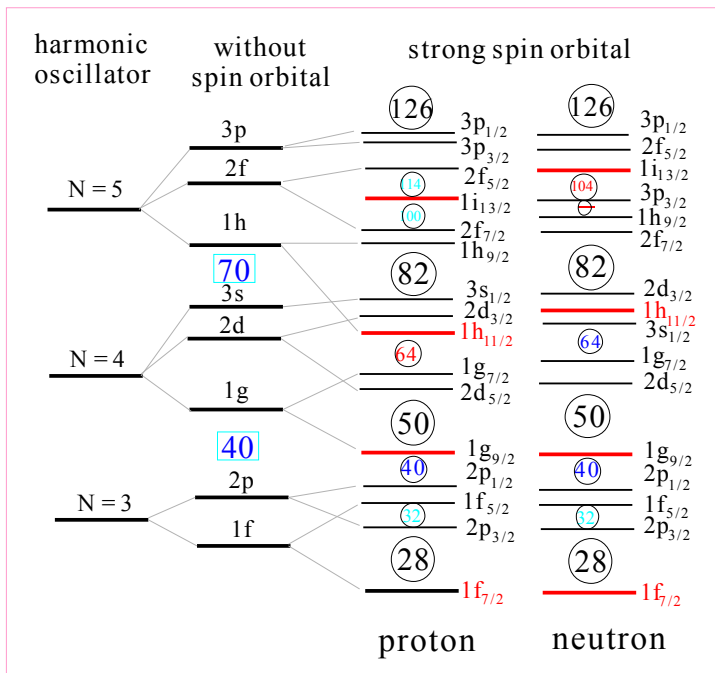
Mirror 거울

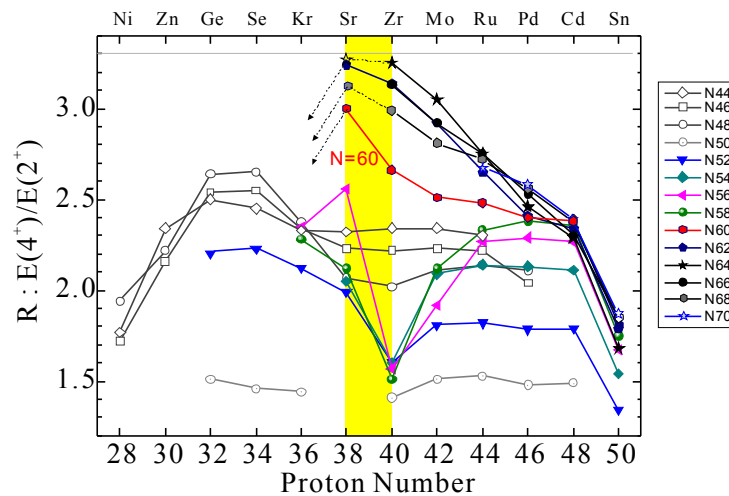
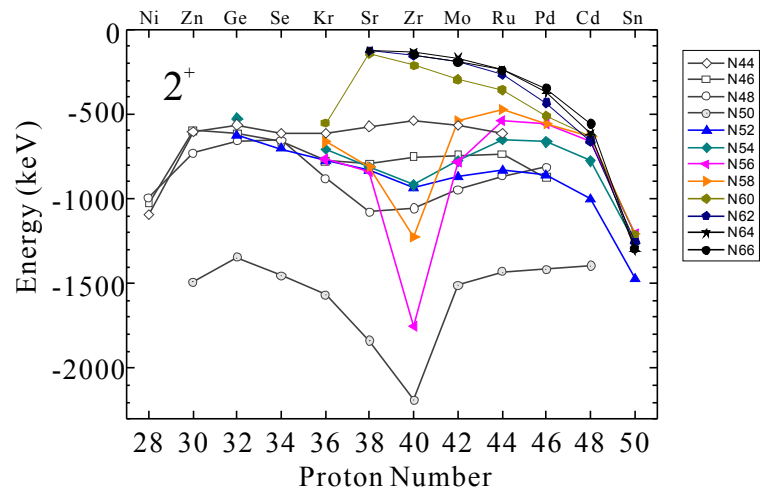
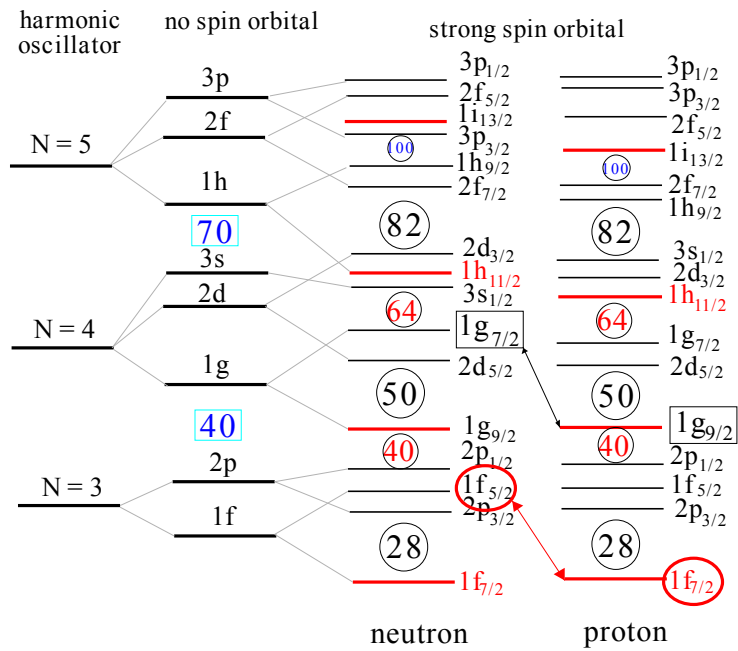


Mirror 거울



Symmetry

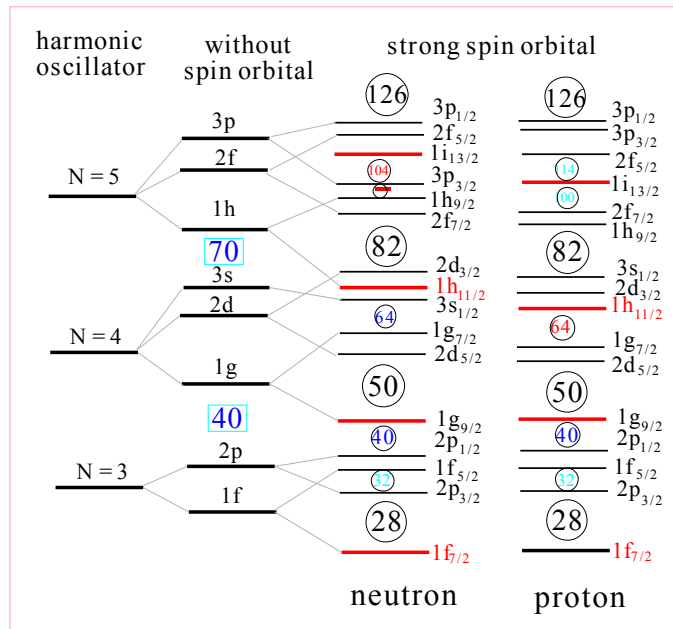




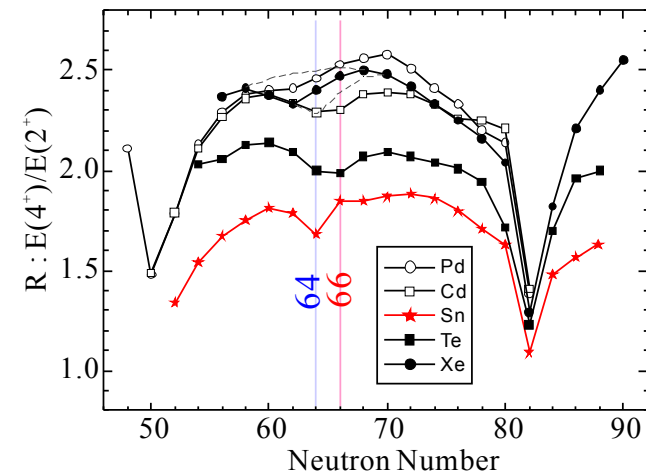
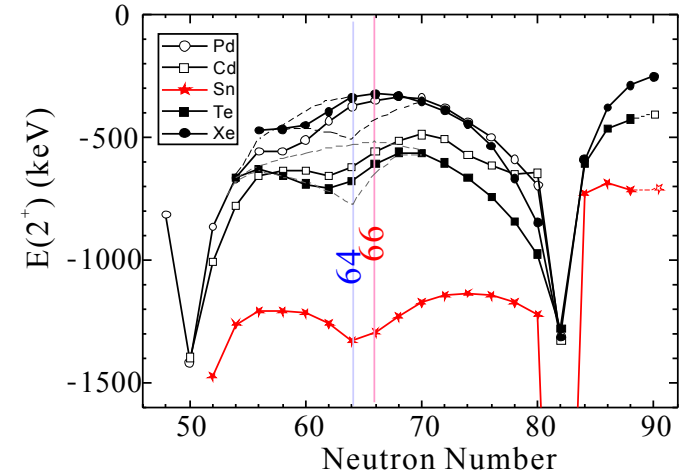
## 2. 시작점

### Nuclear shapes and their phases

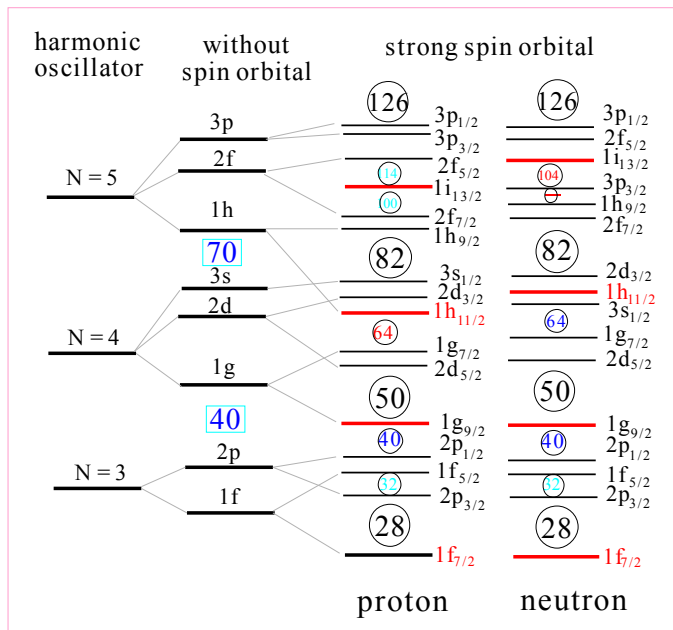
Atomic nuclei have a shell structure under which have favored configurations



What a similarity between energy and shape



## Reinforcing deformations

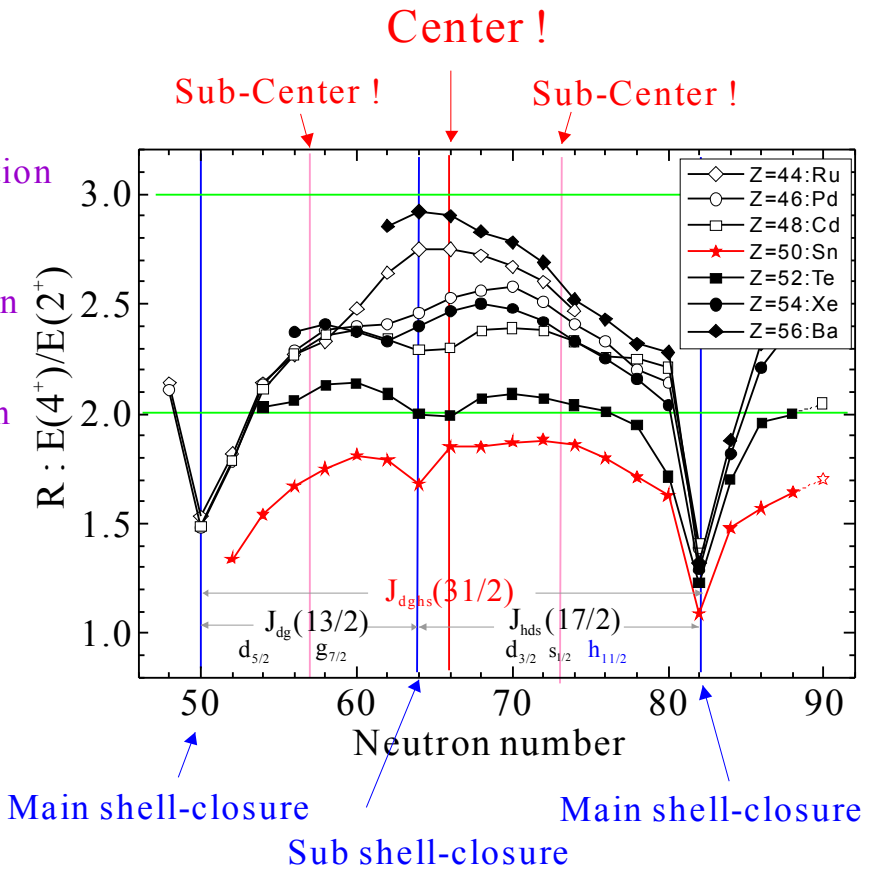


large axial deformation

non axial deformation

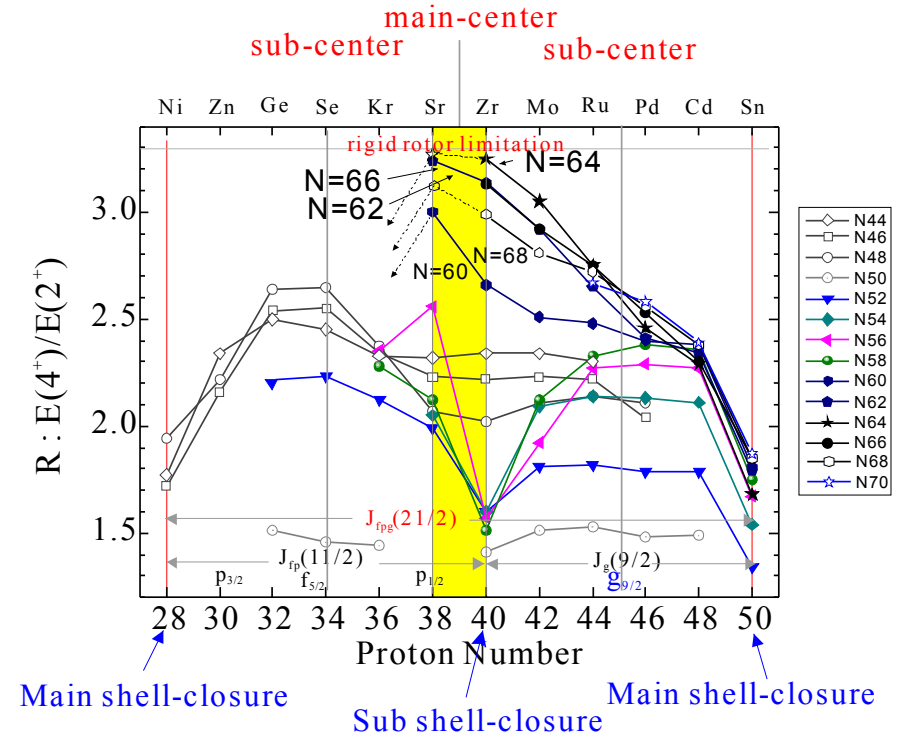
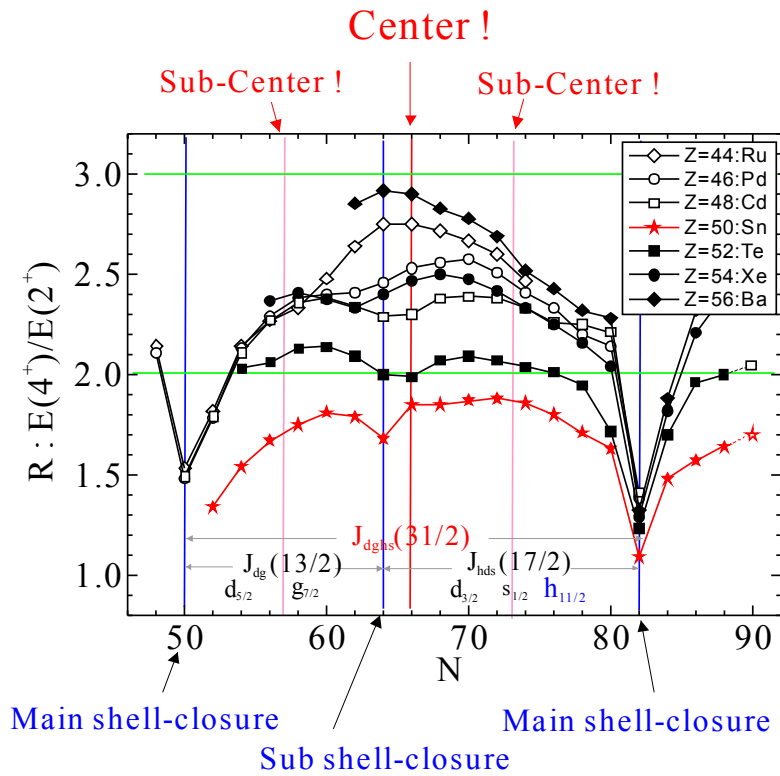
quadrupole vibration

spherical



## Pseudo-shell configurations

# Networking between neutrons and protons





### 3. 출발선에 선 **우리들의** 핵종들

아궁이와 불쏘시개



## Measurement of $^{77,79}\text{Se}(d, p)^{78,80}\text{Se}$ reactions as a surrogate for $^{79}\text{Se}(n, \gamma)^{80}\text{Se}$ reaction

N. Imai,<sup>\*1</sup> M. Dozono,<sup>\*1</sup> S. Michimasa,<sup>\*1</sup> T. Sumikama,<sup>\*2</sup> S. Ota,<sup>\*1</sup> S. Hayakawa,<sup>\*1</sup> K. Iribe,<sup>\*3</sup> C. Iwamoto,<sup>\*1</sup> S. Kawase,<sup>\*4</sup> K. Kawata,<sup>\*1,\*2</sup> N. Kitamura,<sup>\*1</sup> S. Masuoka,<sup>\*1</sup> K. Nakano,<sup>\*4</sup> P. Schrock,<sup>\*1</sup> D. Suzuki,<sup>\*2</sup> R. Tsunoda,<sup>\*1</sup> K. Wimmer,<sup>\*5</sup> D.S. Ahn,<sup>\*2</sup> O. Beliuskina,<sup>\*1</sup> N. Chiga,<sup>\*2</sup> N. Fukuda,<sup>\*2</sup> E. Ideguchi,<sup>\*6</sup> K. Kusaka,<sup>\*2</sup> H. Miki,<sup>\*7</sup> H. Miyatake,<sup>\*8</sup> D. Nagae,<sup>\*2</sup> M. Nakano,<sup>\*9</sup> S. Ohmika,<sup>\*2</sup> M. Ohtake,<sup>\*2</sup> H. Otsu,<sup>\*2</sup> H.J Ong,<sup>\*6</sup> S. Sato,<sup>\*9</sup> H. Shimizu,<sup>\*1</sup> Y. Shimizu,<sup>\*2</sup> H. Sakurai,<sup>\*2,\*5</sup> X. Sun,<sup>\*2</sup> H. Suzuki,<sup>\*2</sup> M. Takaki,<sup>\*1</sup> H. Takeda,<sup>\*2</sup> S. Takeuchi,<sup>\*7</sup> T. Teranishi,<sup>\*3</sup> Y. Watanabe,<sup>\*4</sup> Y.X. Watanabe,<sup>\*8</sup> H. Yamada,<sup>\*7</sup> H. Yamaguchi,<sup>\*1</sup> L. Yang,<sup>\*1</sup> R. Yanagihara,<sup>\*6</sup> K. Yoshida,<sup>\*2</sup> Y. Yanagisawa,<sup>\*2</sup> and S. Shimoura<sup>\*1</sup>

To design a facility for decommissioning the spent fuel from nuclear power plants containing long-lived fission products (LLFPs), more nuclear reaction data is needed. Within the ImPACT program, thus far several nuclear reactions of LLFPs produced by Bi-gRIPS impinging on nuclear and proton targets have been measured.<sup>1)</sup> Because of the longer mean free path, the transmutation with neutrons can be applied more efficiently. However, since both the neutron and the LLFPs are unstable, the measurement of the neutron-induced cross section requires a neutron facility, in addition to enriched radioactive targets. Instead, the reaction cross-section can be determined in an indirect way employing a surrogate reaction.

**PTEP**

Prog. Theor. Exp. Phys. 2019, 043D02 (11 pages)  
DOI: 10.1093/ptep/ptz028

### Angle-tunable wedge degrader for an energy-degrading RI beamline

Jongwon Hwang<sup>1,\*</sup>, Shin'ichiro Michimasa<sup>1</sup>, Shinsuke Ota<sup>1</sup>, Masanori Dozono<sup>1</sup>, Nobuaki Imai<sup>1</sup>, Koichi Yoshida<sup>2</sup>, Yoshiyuki Yanagisawa<sup>2</sup>, Kensuke Kusaka<sup>2</sup>, Masao Ohtake<sup>2</sup>, Deuk Soon Ahn<sup>2</sup>, Olga Beliuskina<sup>1</sup>, Naoki Fukuda<sup>2</sup>, Chihiro Iwamoto<sup>1</sup>, Shoichiro Kawase<sup>3</sup>, Keita Kawata<sup>1</sup>, Noritaka Kitamura<sup>1</sup>, Shoichiro Masuoka<sup>1</sup>, Hideaki Otsu<sup>2</sup>, Hiroyoshi Sakurai<sup>2</sup>, Philipp Schrock<sup>1</sup>, Toshiyuki Sumikama<sup>2</sup>, Hiroshi Suzuki<sup>2</sup>, Motonobu Takaki<sup>1</sup>, Hiroyuki Takeda<sup>2</sup>, Rieko Tsunoda<sup>1</sup>, Kathrin Wimmer<sup>4</sup>, Kentaro Yako<sup>1</sup>, and Susumu Shimoura<sup>1</sup>

# 중이온가속기 KoRIA와 천체핵물리학

한국물리학회지 "새물리", Volume 60, Number 8, 2010년 8월

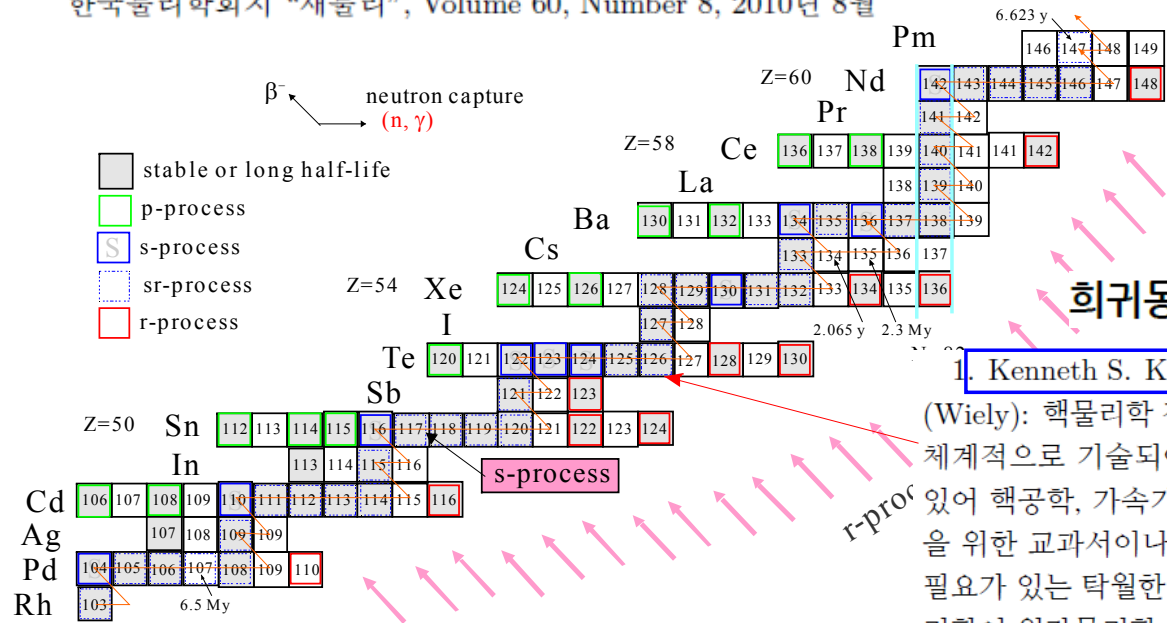
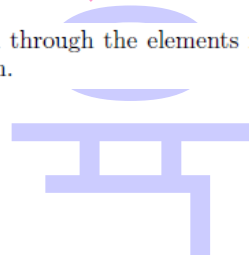


Fig. 17. The s-process path through the elements from Rh to Pm [1]. Notice that like  $^{107}\text{Pd}$ ,  $^{135}\text{Cs}$ , and  $^{147}\text{Pm}$ .



## 희귀동위원소 가속기와 핵과학

1. Kenneth S. Krane, "Introductory Nuclear Physics" (Wiley): 핵물리학 전반에 걸친 이론과 실험 그리고 개념이 체계적으로 기술되어 있음. 핵물리 응용분야까지 다루고 있어 핵공학, 가속기 물리학자들에게도 추천함. 학부과정을 위한 교과서이나 최고의 핵물리학 전문가도 정독을 할 필요가 있는 탁월한 참고서적임. 특히 응용편 16장은 핵물리학이 원자물리학 연구에 어떻게 연결되는지를 아름답게 설명하고 있음.



New Physics: Sae Mulli,  
Vol. 66, No. 12, December 2016, pp. 1480~1490  
<http://dx.doi.org/10.3938/NPSM.66.1480>

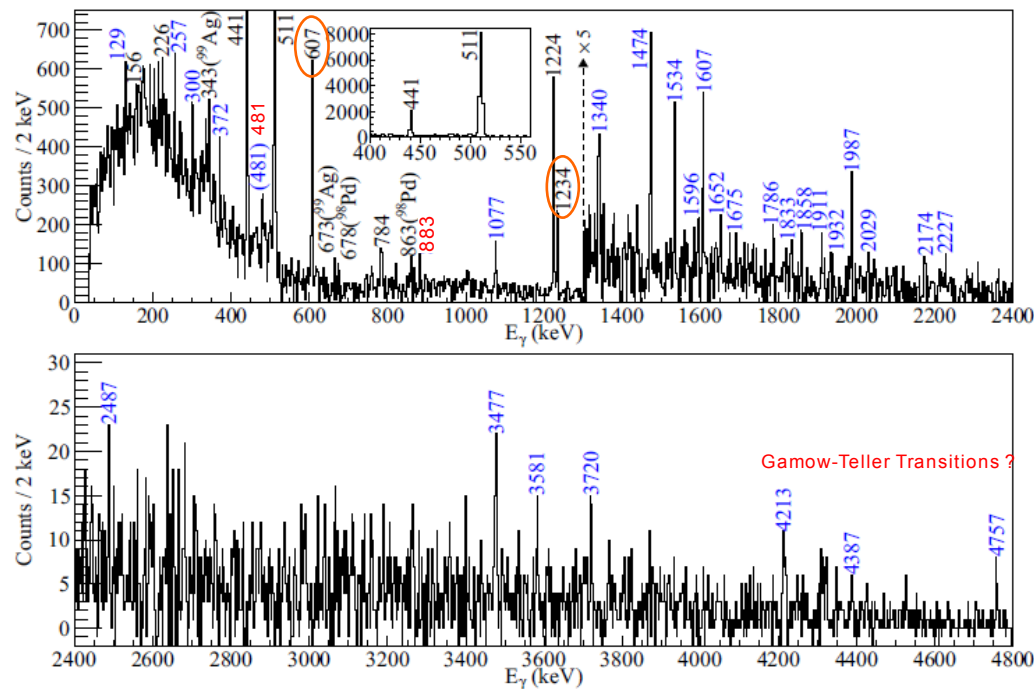


FIG. 2. Background-subtracted  $\gamma$ -ray spectra of  $\beta$ -decay events correlated between 0 and 5 s after  $^{99}\text{In}$  implantation. The peaks labeled in black correspond to the previously observed  $\gamma$  rays in  $^{99}\text{Cd}$  [8] and other background contaminants as labeled. New transitions from this decay

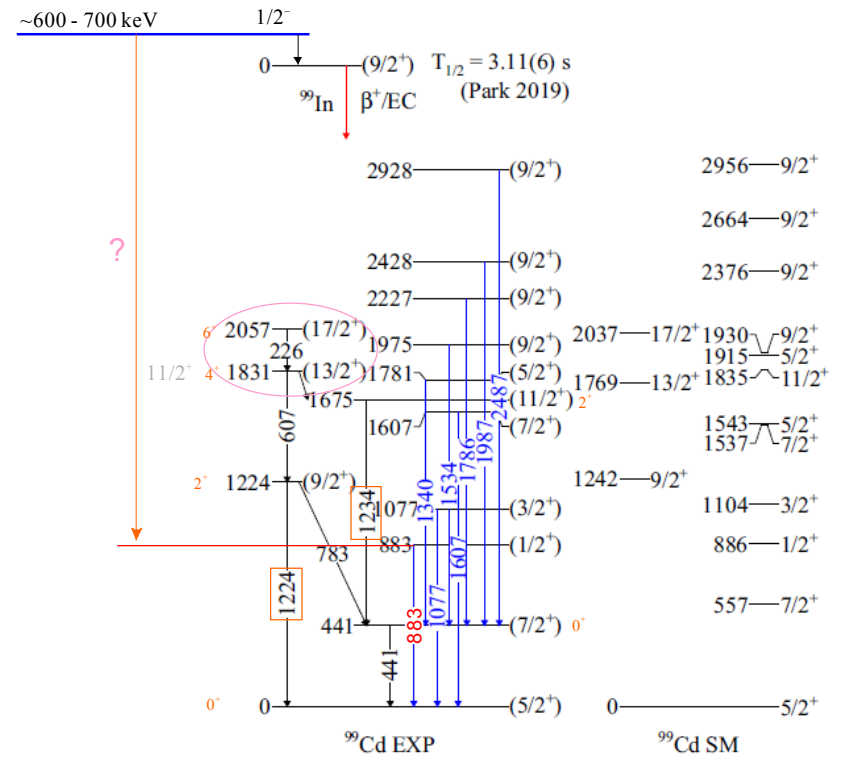
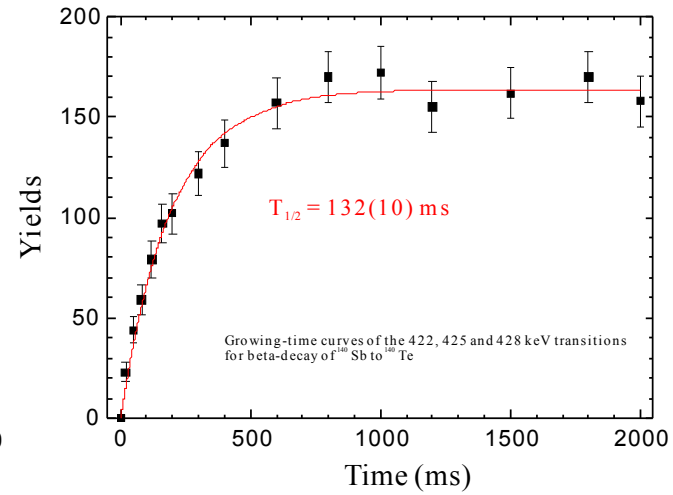
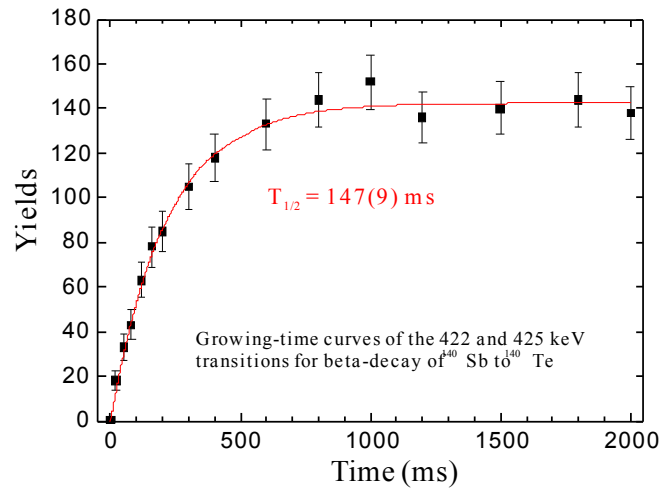
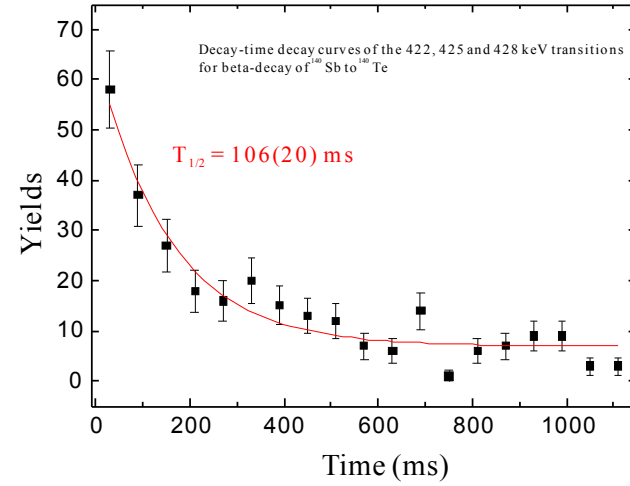
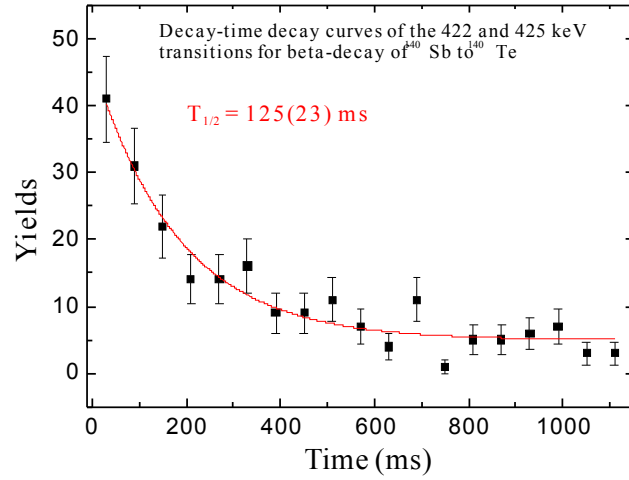


FIG. 4. Level schemes of  $^{99}\text{Cd}$  from the  $\beta\gamma$  spectroscopy of  $^{99}\text{In}$ .

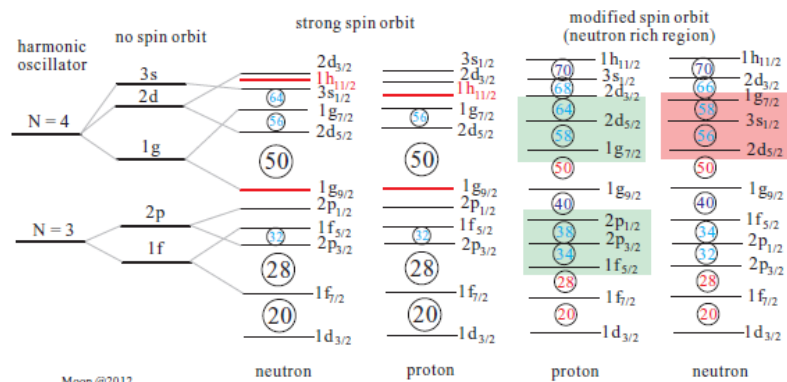


Moon@2015.10.21.









Moon @2012

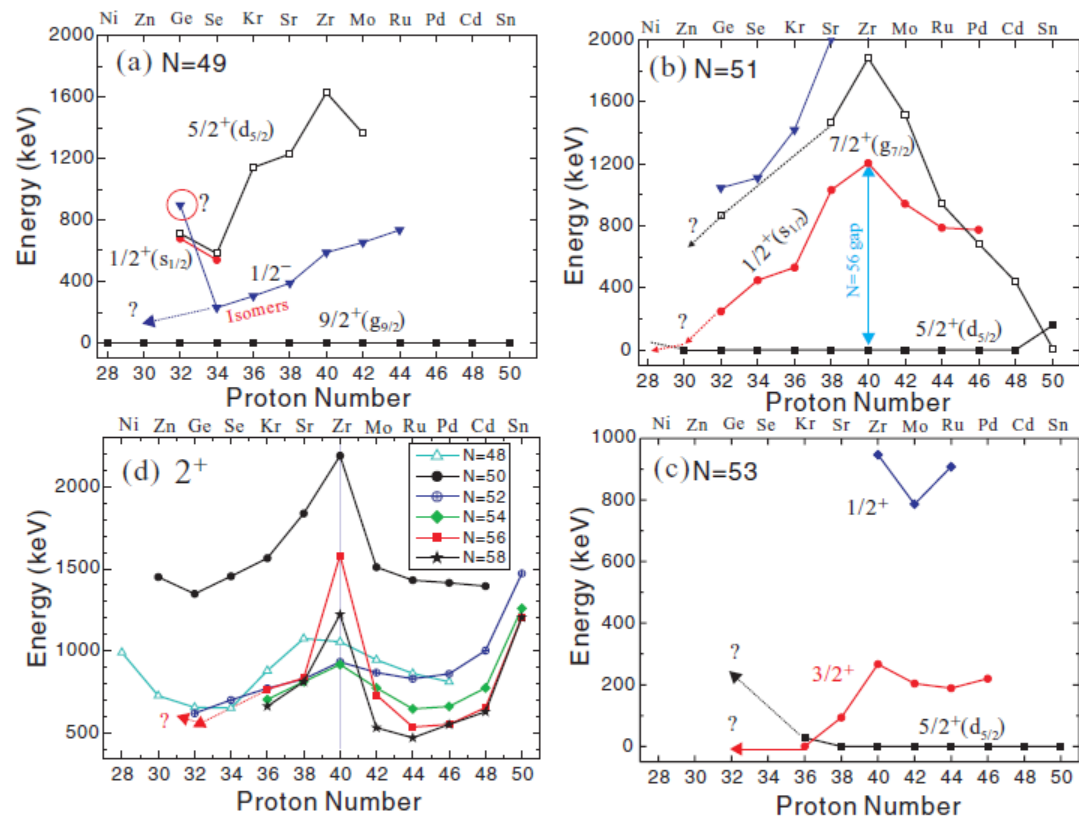
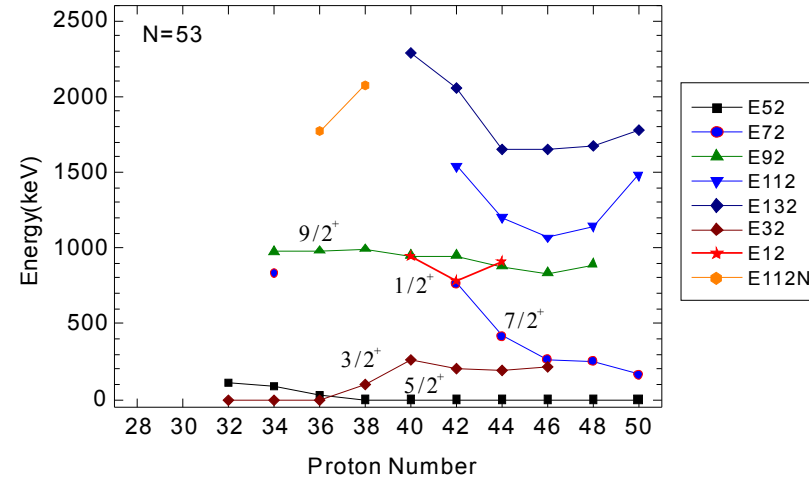
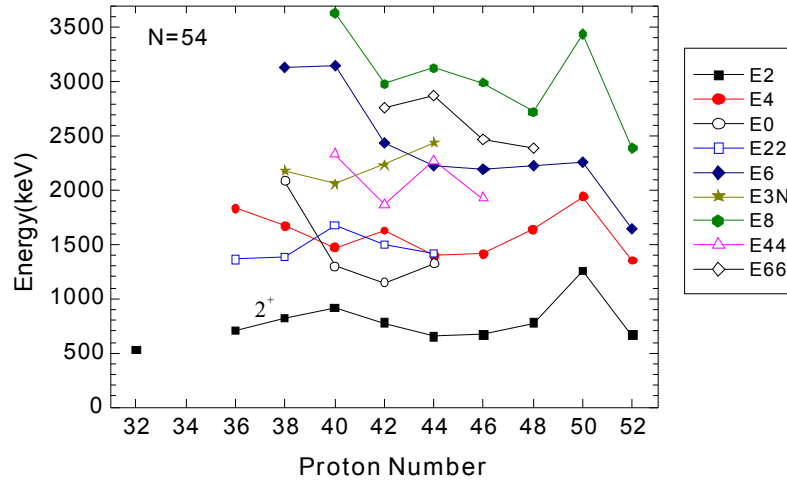
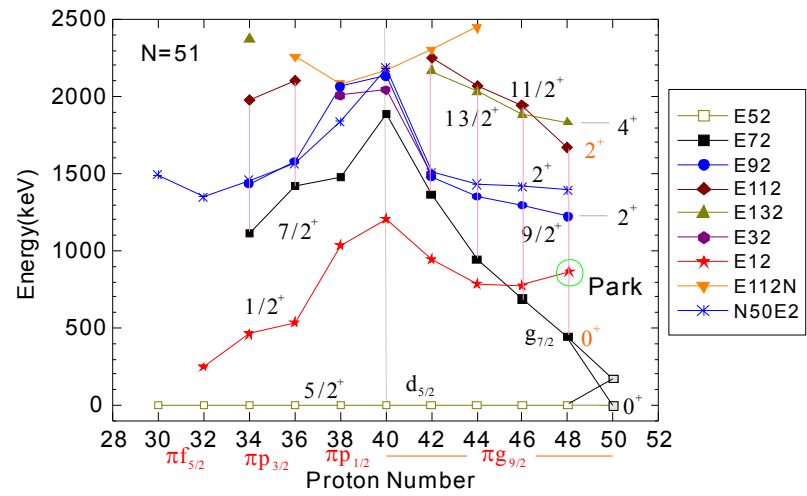
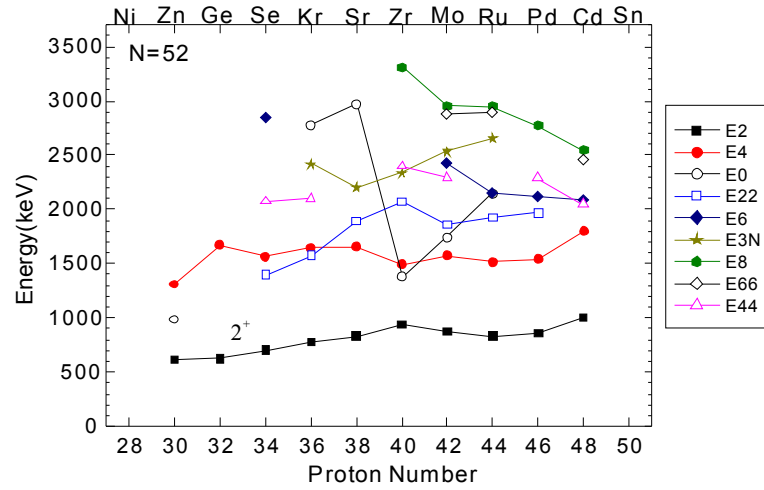
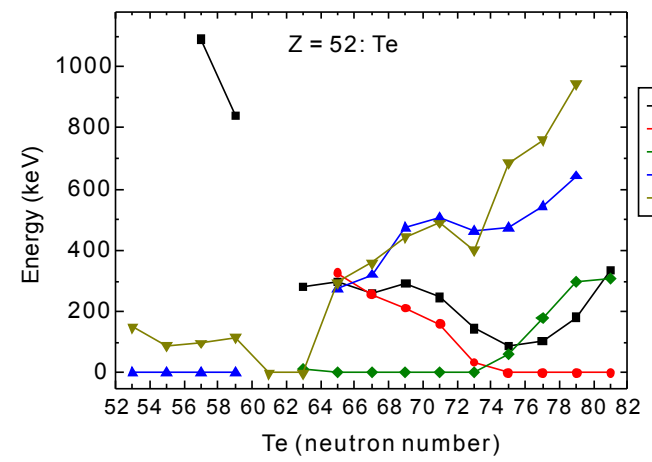
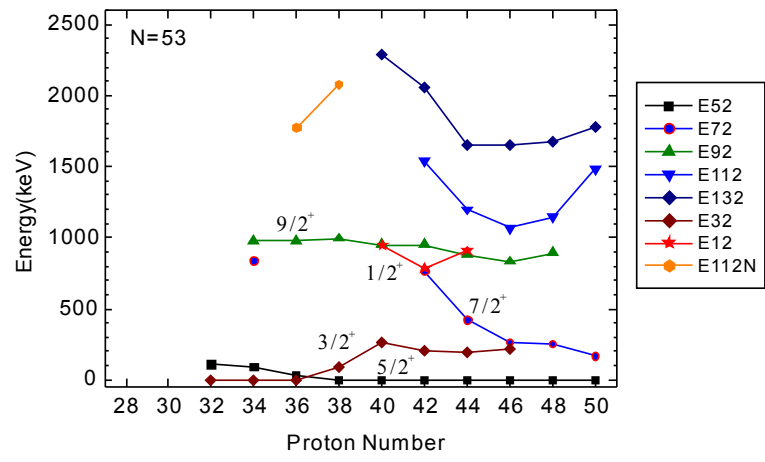
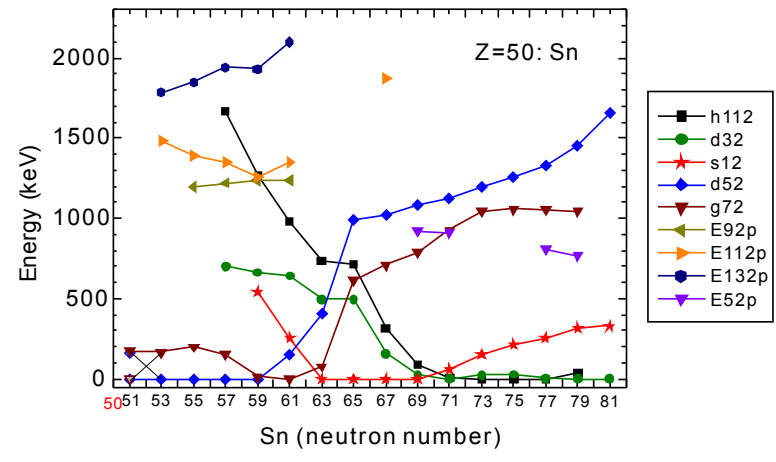
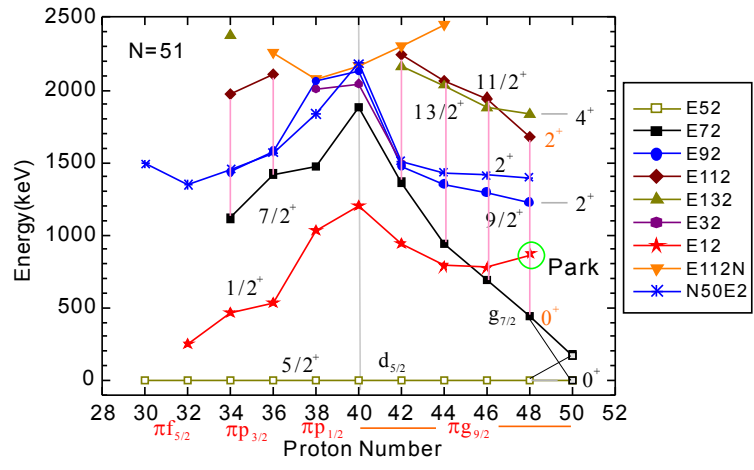
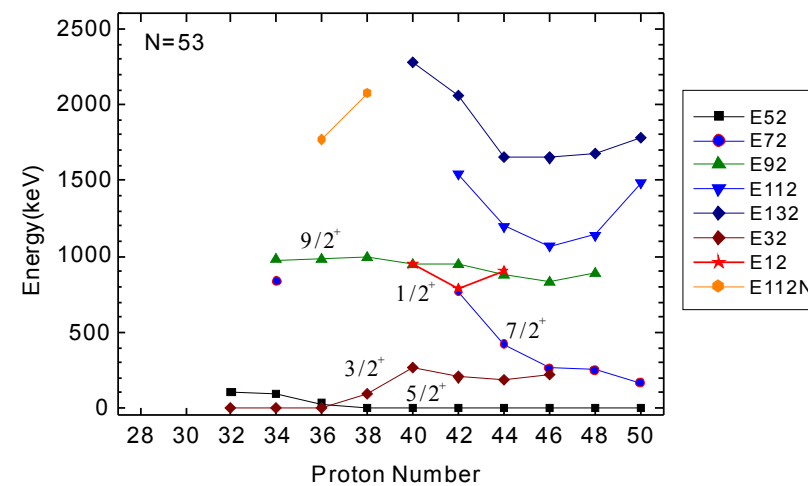
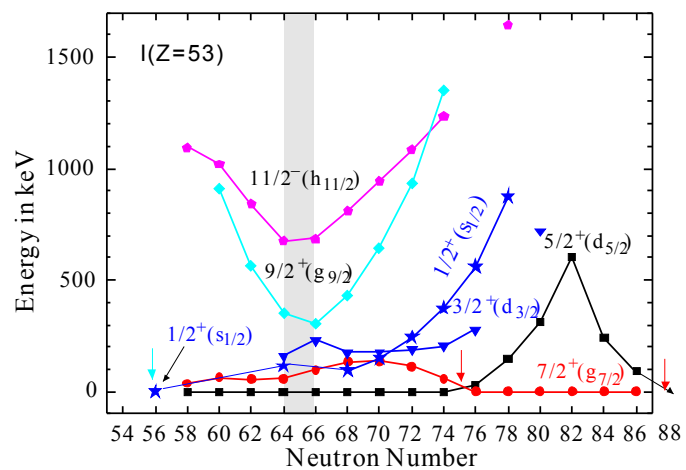
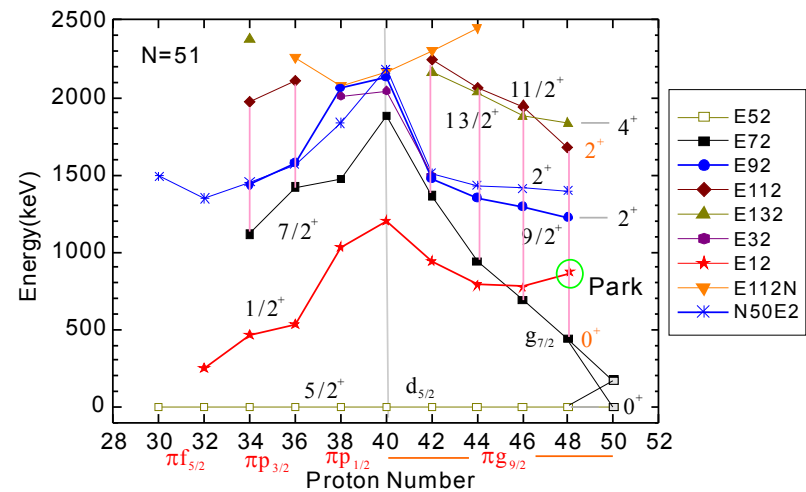
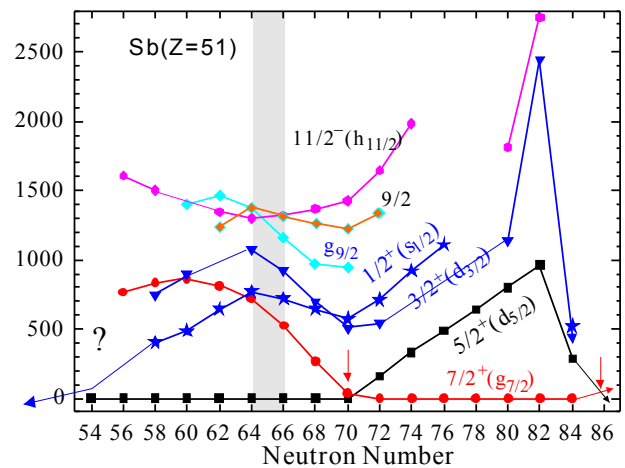


FIG. 22. Systematics of the ground and the excited states of interest in odd N = 49, 51, and 53 nuclei as a function of proton number. For comparison and discussion, the associated systematics of the first 2<sup>+</sup> states in even-even nuclei is also included.

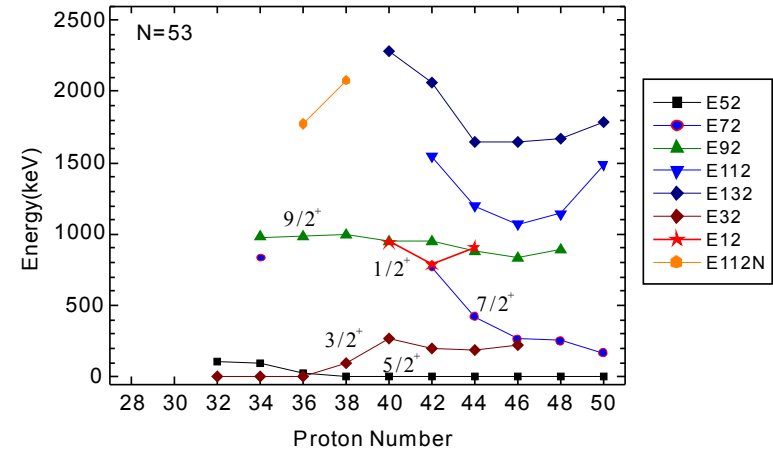
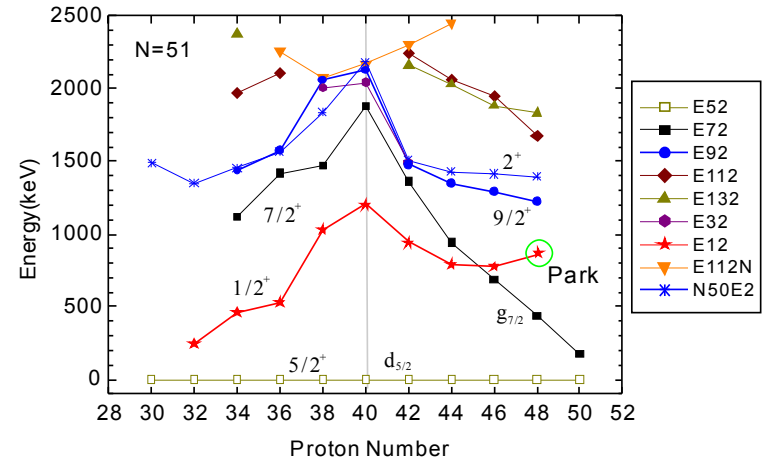
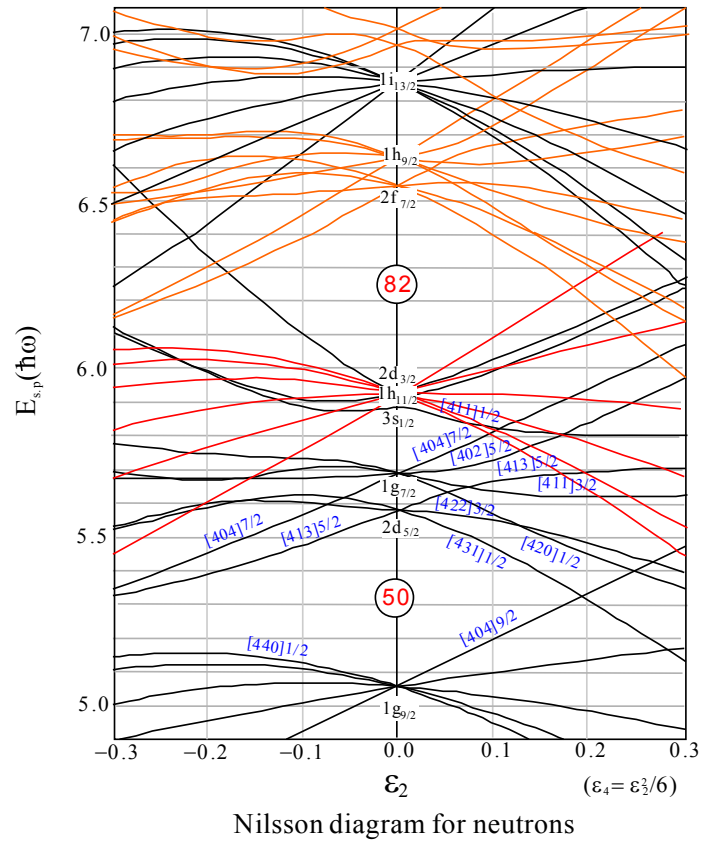
2020. 6. 8.

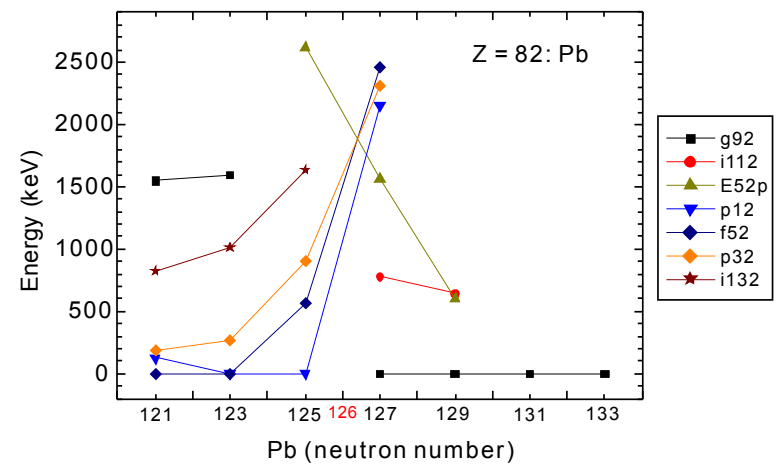
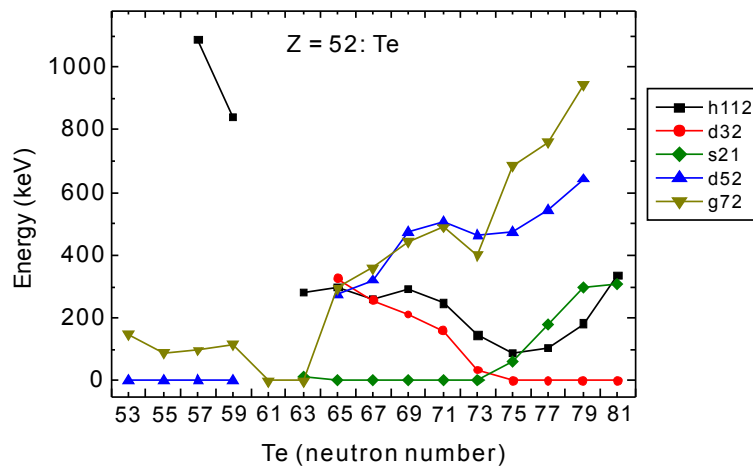
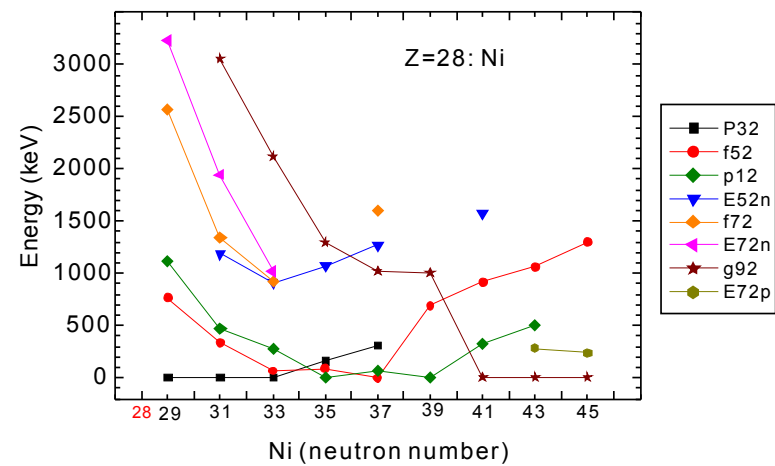
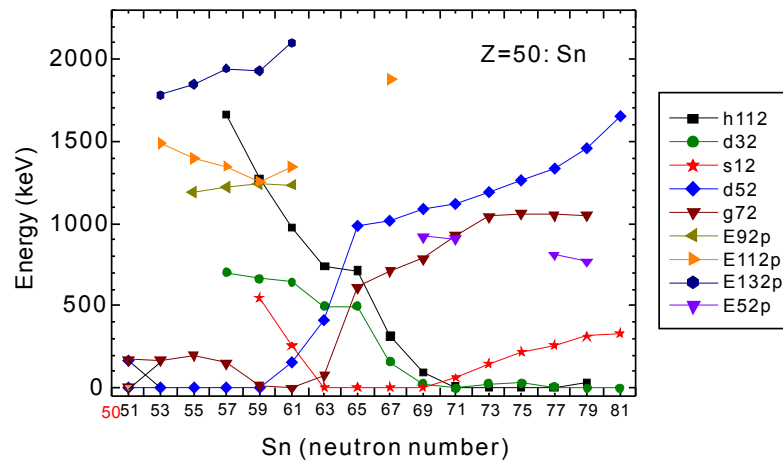






유행하는 spherical shell model이 다가 아니다





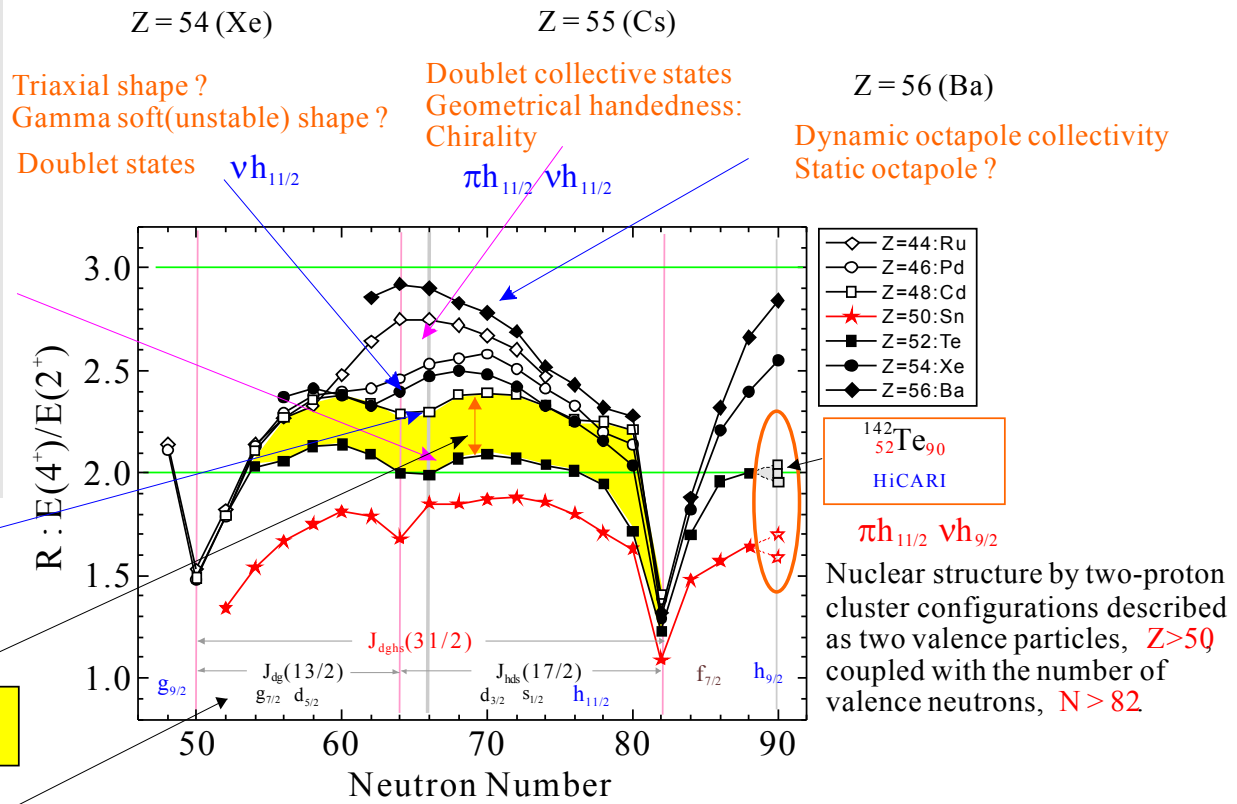
# Variety of nuclear structures for $Z = 48$ to $56$ , $50 < N < 82$

- 1  $Z = 53$  (I)  
 Doublet collective states  
 Shape coexistence  
 $\pi h_{11/2}$   $\pi h_{11/2} \nu h_{11/2}$
- 2  $Z = 52$  (Te)  
 Structure of two valence protons  
 : a big puzzle to be solved  
 $\pi g_{7/2}$   $\pi d_{5/2}$
- 3  $Z = 51$  (Sb) Isomers  
 $\pi h_{11/2} \nu h_{11/2}$

$Z = 48$  (Cd)  
 Collectivity still unclear  
 : Triaxial rotator or vibrator ?

$\pi g_{9/2}$   $\nu h_{11/2}$   
 Notice a large difference between  
 $Z = 48$  and  $Z = 52$

pseudo-shell concept  
 $l=2, l=4 \Rightarrow \tilde{l}=3$   
 : doublet shell structure



## 4. 갈 길



Don't stay a particular ridge of your own interest, but look at other domains in nuclear many-body quantum systems, even at different branches; chemistry and biology.

I hope the presentation make you feel free to extrapolate and to speculate about where you go next.

Foresight ? but also backsight !  
Background ? but also foreground !  
Forecast ? but also backcast !

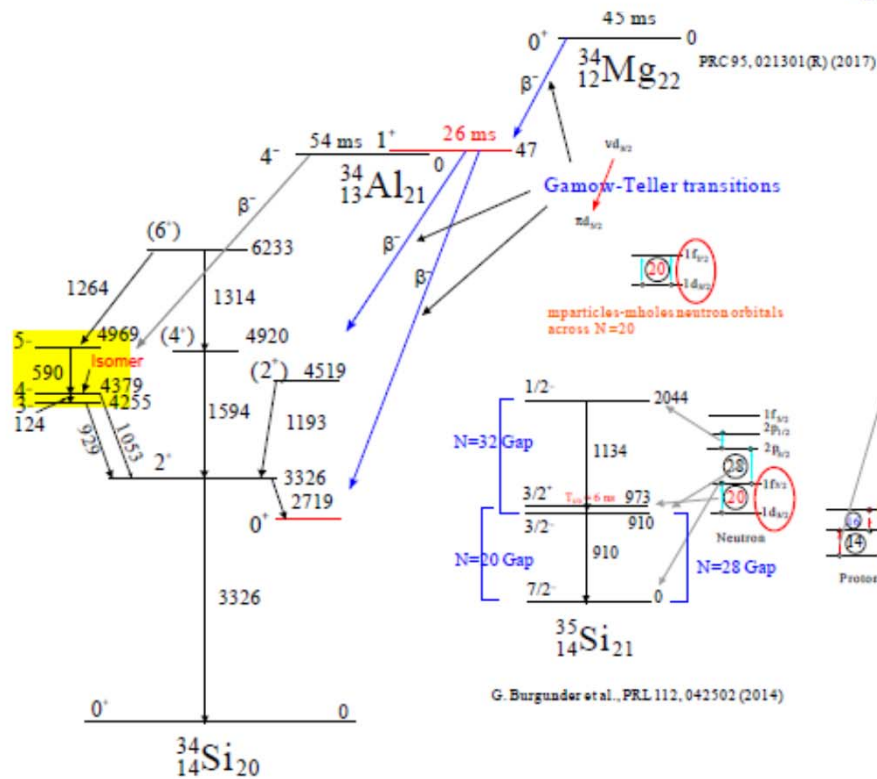
The author shows how our **personalities** reflect the biological mechanisms underlying thought and emotion and how **behavioral eccentricities** may be traced to abnormalities in an individual brain.  
-mapping the mind-



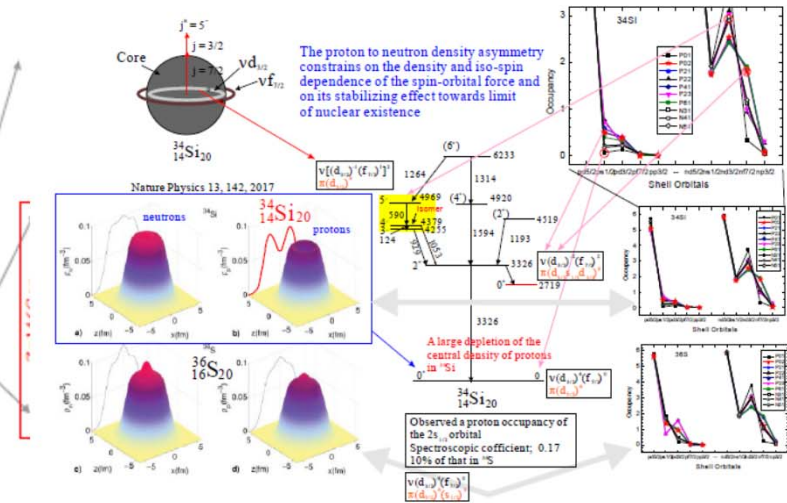


## **An Episode**

## Exotic facets in the Z(proton) = 14 and N(neutron) = 20 system: <sup>34</sup>Si



G. Burgunder et al., PRL 112, 042502 (2014)



PRC 93, 034333 (2016)

### The deformed $0^+$ state in $^{34}\text{Si}$

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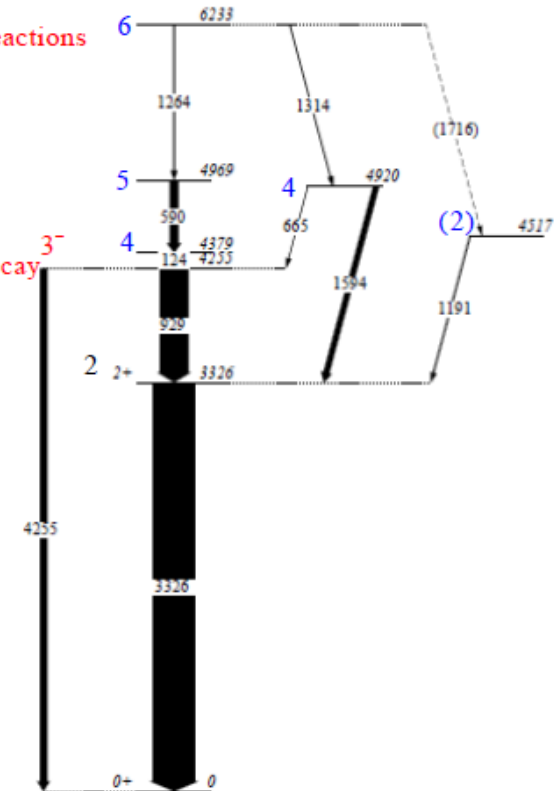
Conversion electron measurements should have made

**Abstract.** The energy of the lowest deformed 2-particle 2-hole (2p2h)  $0^+$  state in even-even  $N = 20$  nuclei is a key observable directly related to the size of the neutron  $N = 20$  shell closure.  $^{34}\text{Si}$ , with 14 protons and 20 neutrons, lies at the boundary of the “island of inversion”, where the deformed 2p2h  $0^+$  state is the ground state in even- $A$  nuclei. In  $^{34}\text{Si}$ , the 2p2h  $0^+$  state is expected to be particularly low lying - in some theories it is even predicted to lie below the first  $2^+$  state. While there have been a number of attempts, using various techniques, no experiment to date has been able to firmly locate the  $^{34}\text{Si}$  2p2h  $0^+$  state although a number of candidates have been suggested. Here we present, for the first time, data obtained from a fusion-evaporation reaction  $^{18}\text{O}(^{18}\text{O}, 2p)$  to produce  $^{34}\text{Si}$ . Gammasphere and Microball were used to detect  $\gamma$ - $\gamma$  coincidences and charged particles (two protons), respectively. The increased sensitivity of this experiment using  $\gamma$ - $\gamma$  coincidences and a high charged-particle detection efficiency helped to exclude previously reported candidates and provided a stringent limit on the anticipated  $\gamma$  decay from the first  $2^+$  state to the 2p2h  $0^+$  state.

Fusion-evaporation reactions produce mainly

Yrast states

determined by beta decay



# Level structure of the double-shell closure system with $Z = 14$ and $N = 20$ : $^{34}\text{Si}$

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(Dated: January 2, 2019)

Level structure of the double-magic nucleus  $^{34}\text{Si}$  ( $Z = 14$ ,  $N = 20$ ) has been investigated by evaluating the available data. On the basis of experimental results from the beta-decay and fusion-evaporation reactions, we have established the level scheme as assigning spin-parities up to  $6_1^+$  at 6233 keV. The energy ratio of the first  $4^+$  state to the first  $2^+$  state,  $E(4^+/2^+)$  turns out to be 1.48, which is consistent with values of the double-magic nuclei such as  $^{68}\text{Ni}$  ( $Z = 28$ ,  $N = 40$ ), 1.55. This nucleus, for a long time, has attracted much attention because of, on one side, a proton bubble structure at the ground state and, on the other side, a deformation at the second  $0^+$  state,  $0_2^+$ . By a comparison of the constructed level scheme with the shell model calculations, we describe the emerging structures in the ground  $0^+$ , second  $0^+$ , and negative-parity  $3^-$  states within the framework of shell model context. We propose a deformed rotational band with the cascading  $6_2^+ - 4_1^+ - 2_1^+$  transitions built on the  $0_2^+$  state.

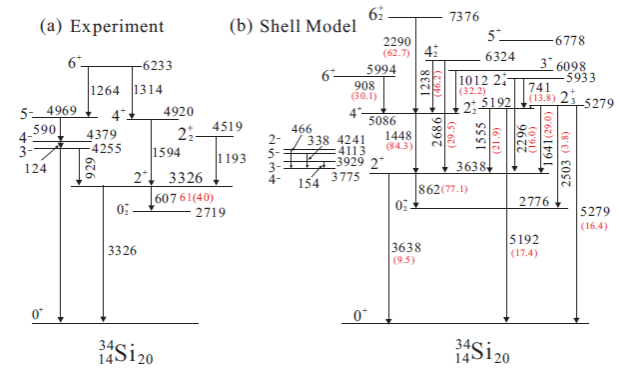


FIG. 3: (Color online) (a) Level scheme of  $^{34}\text{Si}$  proposed by the present work. (b) The predicted level scheme of  $^{34}\text{Si}$  by the large-scale shell-model calculations over the space of  $d_{5/2}$ ,  $s_{1/2}$ ,  $d_{3/2}$ ,  $f_{7/2}$ , and  $p_{3/2}$  for both protons and neutrons. Numbers in parentheses are the expected electric quadrupole transition strengths,  $B(E2; J+2 \rightarrow J)$ , in  $e^2 \text{fm}^4$ . The experimental value in (a) is from [4].

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## Northern boundary of the “island of inversion” and triaxiality in $^{34}\text{Si}$

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## Normal and intruder configurations in $^{34}\text{Si}$ populated in the $\beta^-$ decay of $^{34}\text{Mg}$ and $^{34}\text{Al}$

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(IDS Collaboration)



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### E. Triaxiality in $^{34}\text{Si}$ ?

A recent study [20] claimed evidence of triaxiality in  $^{34}\text{Si}$  based on the decay pattern of the  $2_2^+$  state at 4519 keV to the  $0_2^+$  level by a 1800-keV  $\gamma$ -ray transition, in addition to its already known decays to the  $0_1^+$  and  $2_1^+$  states. Unfortunately,

The present paper concludes that (1) the present experimental and theoretical results do not support the presence of triaxially deformed structures in  $^{34}\text{Si}$ , being consistent with two estimates, based on different theory approaches, which point to a pronounced  $\gamma$  softness, in line with the potential energy surface (PES) calculations discussed in Ref. [20]; (2) more precise Coulomb excitation measurements are required in order to lower the uncertainty for the known  $B(E2)$  values and to determine the ones corresponding to the newly identified  $2^+$  states in  $^{34}\text{Si}$ .

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Ms. No.: PLB-D-19-00005  
 Level structure of the double-shell closure system with  $Z = 14$  and  $N = 20$ :  $^{34}\text{Si}$

Dear Professor Changbum Moon,

I am writing to you in regard to your above-referenced manuscript which we invited you to revise and resubmit for continued publication consideration at Physics Letters B.

I regret to have to inform you that the deadline set for the revision of your manuscript has long passed and we have not received any update on the status of your manuscript.

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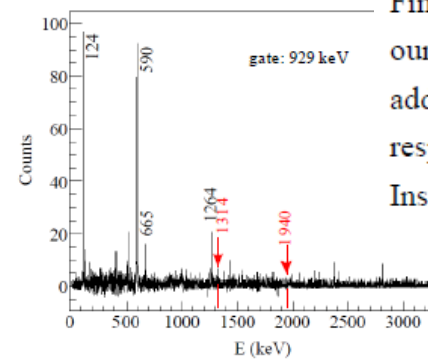
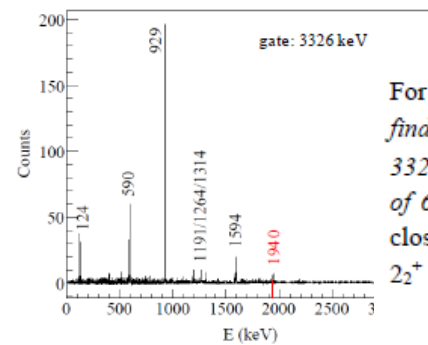
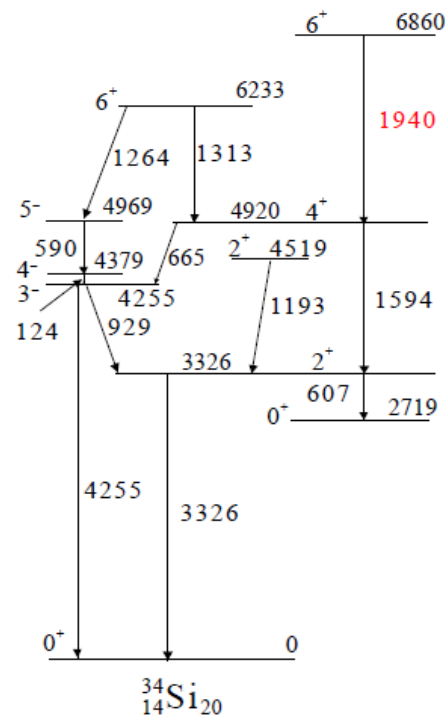
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We hope you will revise and resubmit your paper soon and we appreciate you helping us update our records.

Yours sincerely,

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For confirming our suggestion, the second  $6^+$  state will be identified by an experiment. *Interestingly, we find a  $\gamma$ -ray peak near 1940 keV on Figure 2 in [5] where the coincidence  $\gamma$ -ray spectra gated on the 3326-keV and 929-keV transitions are displayed. We suggest that this peak might be the  $\gamma$ -ray transition of  $6_2^+$  state, leading to the 6860-keV level, to the  $4^+$  state at 4920 keV. It is also worthwhile to know a close resemblance between the collective bands, the  $6_2^+ - 4_1^+ - 2_1^+ - 0_2^+$  sequence in  $^{34}\text{Si}$  and the  $6_2^+ - 4_1^+ - 2_2^+ - 0_2^+$  sequence in  $^{38}\text{Ar}$ .*

Finally, let us notice a recent paper published during the revision. This paper supports our result and is certainly consistent with our discussion. We include this paper as a note added in proof, which is put in a reference number, 17. Here we would not like to any response to the insistence, such as a tri-axial shape, raised by the authors in Ref. 9. Instead, we are very glad to see conclusions made by the authors in Ref. 17.

Figure 2. Proposed level scheme by considering the 1940-keV transition in ref. 5.

## **Level structure of the double-shell closure system with $Z = 14$ and $N = 20$ : $^{34}\text{Si}$**

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(Submit: 2 January 2019, Resubmit: 12 August 2020)

Level structure of the double-magic nucleus  $^{34}\text{Si}$  ( $Z = 14$ ,  $N = 20$ ) has been investigated by evaluating the available data. On the basis of experimental results from the beta-decay and fusion-evaporation reactions, we have established the level scheme as assigning spin-parities up to  $6_1^+$  at 6233 keV. The energy ratio of the first  $4^+$  state to the first  $2^+$  state,  $E(4^+/2^+)$  turns out to be 1.48, which is consistent with values of the double-magic nuclei such as  $^{68}\text{Ni}$  ( $Z = 28$ ,  $N = 40$ ), 1.55. This nucleus, for a long time, has attracted much attention because of, on one side, a proton bubble structure at the ground state and, on the other side, a deformation at the second  $0^+$  state,  $0_2^+$ . By a comparison of the constructed level scheme with the shell model calculations, we describe the emerging structures in the ground  $0^+$ , second  $0^+$ , and negative-parity  $3^-$  states within the frame work of shell model context. We propose a deformed rotational band with the cascading  $6_2^+ - 4_1^+ - 2_1^+$  transitions built on the  $0_2^+$  state.